### Formal Verification of the eBPF Verifier with Agni

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Joint work with Harishankar Vishwanathan, Matan Shachnai, and Srinivas Narayana

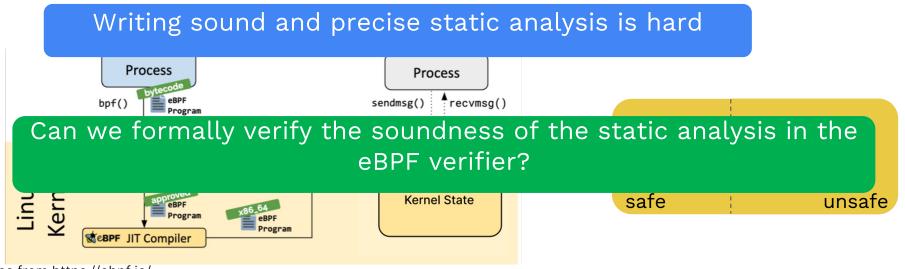


#### eBPF Verifier's Goals: Soundness, Precision, and Speed

Soundness: Unsafe programs should be rejected

Precision: Safe programs shouldn't be rejected

Speed: Minimal load times + Prompt feedback on rejection





#### Static Analyses in the eBPF Verifier and Our Work



- Tnums [CGO '22]: Reasoning about the soundness of bitwise tracking –
   Manually encoded correctness specification and semi-manual verification
- Agni [CAV '23]: Automated reasoning about the soundness and precision of the range analysis + bitwise tracking + their combination
- Agni++[SAS'24]: Fixing the latent unsoundness in the abstract operators

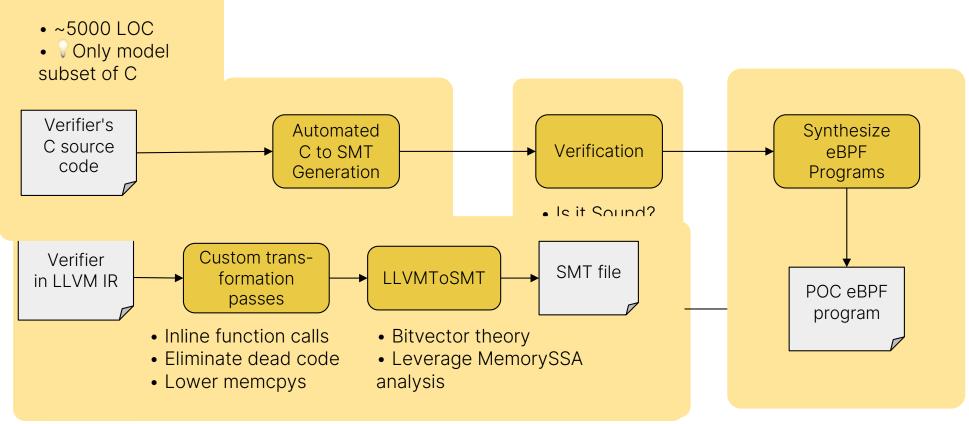


## Tools that can be used to check a patch before it is accepted (e.g., as part of CI)

Thanks to Paul Chaignon for running CI with Agni for the latest bpf-next



#### Overview of the Agni, which "Verifies the Verifier"



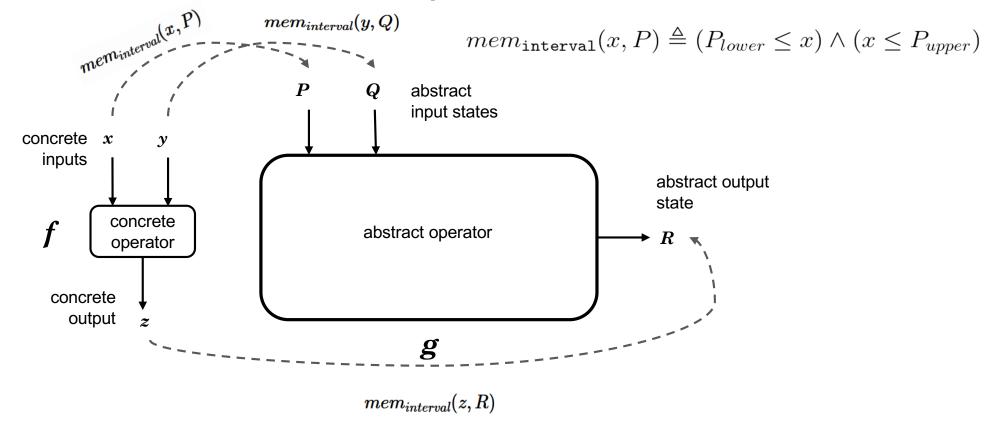


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## Specification at the lowest abstraction level (C code) makes verification challenging



#### When is an Abstract Operator Sound?



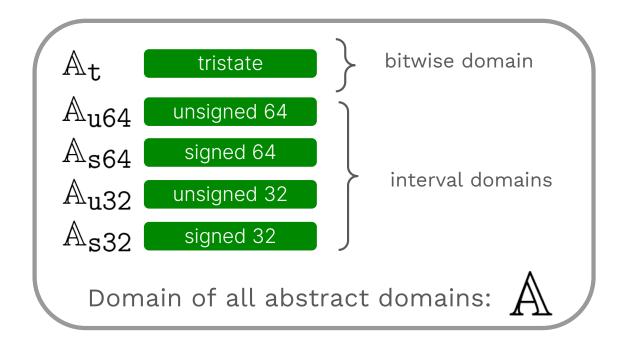


#### Soundness Specification in First Order Logic

$$\forall P, Q \in \mathbb{A}_{\text{interval}}$$
:
 $\forall x, y \in \mathbb{Z}_{64}$ :
 $mem_{\text{interval}}(x, P) \land mem_{\text{interval}}(y, Q) \land z = f(x, y) \land R = g(P, Q) \implies mem_{\text{interval}}(z, R)$ 



#### Value Tracking Abstract Domains in the Linux Kernel







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#### Soundness Specification with Multiple Domains

$$\forall P, Q \in \mathbb{A}$$
:  
 $\forall x, y \in \mathbb{Z}_{64}$ :  
 $mem_{\mathbb{A}}(x, P) \land mem_{\mathbb{A}}(y, Q) \land$   
 $z = f(x, y) \land$   
 $R = g(P, Q) \implies mem_{\mathbb{A}}(z, R)$ 



#### Challenges of Verifying Real World Code

 Performed verification on all kernel versions starting from v4.14



Are all versions truly unsound?



VAZI			( 1
What is the	cause of	verification	failures?

•••	
v5.12	×
v5.13	×
v5.14	×
v5.15	×
•••	×



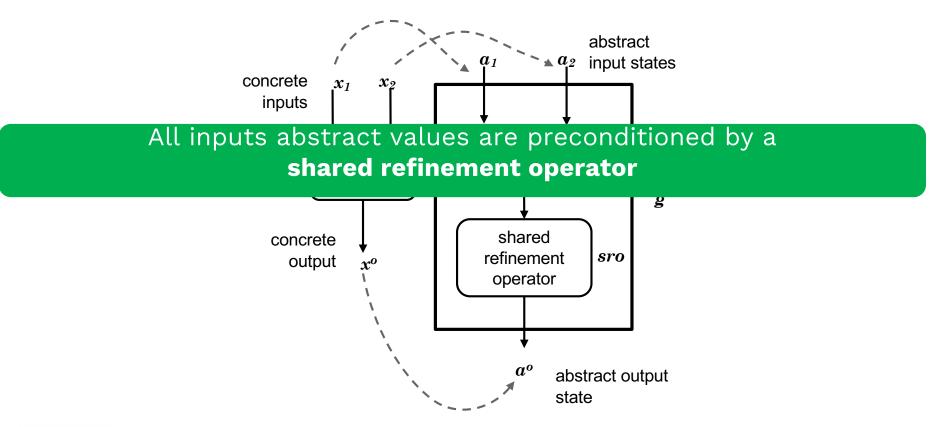
#### Implicit Refinement in the Kernel

```
1.abstract abstractALUOp(
                           concreteOP op, abstract P, abstract Q)
                           abstract R;
                           switch (op) {
                           case BPF_ADD:
                               R = abstractOpADD(P, Q);
                           case BPF_SUB:
                               R = abstractOpSUB(P, Q);
                     9.
                     10.
                          case BPF_MUL:
                                R = abstractOpMUL(P, Q);
                     11.
                     12.
                     13.
                     14.
Shared
                    -15 - - reg_bounds_sync(R);
refinement
                     16.
                            return 0;
operator
                     17.}
```



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#### Shared Refinement Operator Preconditions Abstract States





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#### A Soundness Specification in the presence of SRO

$$\forall P, Q \in \mathbb{A}$$
:  
 $\forall x, y \in \mathbb{Z}_{64}$ :  
 $mem_{\mathbb{A}}(x, P) \land mem_{\mathbb{A}}(y, Q) \land$   
 $z = f(x, y) \land$   
 $R = g(P, Q) \implies mem_{\mathbb{A}}(z, R)$ 

$$\forall P, Q \in \mathbb{A} :$$

$$R_p = sync(P) \land R_Q = sync(Q) \land$$

$$\forall x, y \in \mathbb{Z}_{64} :$$

$$mem_{\mathbb{A}}(x, R_P) \land mem_{\mathbb{A}}(y, R_Q) \land$$

$$z = f(x, y) \land$$

$$R = g(R_P, R_Q) \implies mem_{\mathbb{A}}(z, R)$$



#### Success in Proving the Soundness of Some Kernels

 Proved that all abstract operators in kernels starting from v5.13 are sound

What can we do about unsound versions?

How do we convince developers that these actual bugs?

We generate *actual* eBPF programs using differential program synthesis! [CAV 2023]

Kernel Version	Sound?
v4.14	×
v5.5	×
v5.7	×
	×
v5.12	×
v5.13	
v5.14	
v5.15	
	<b>V</b>
anguages I ah	



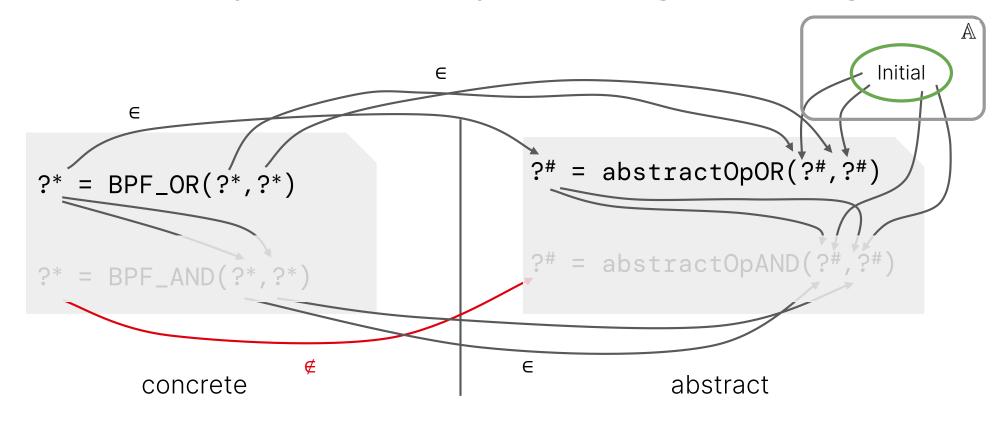
# What does an operator being unsound mean? There exists input abstract states where the operator produces an ill-formed output abstract state



#### Is this "Unsoundness" realizable?



#### Differential Synthesis for Synthesizing eBPF Programs





## Concrete Proof of Concept Programs were helpful to reproducing the bugs



#### When Verification Tools are Continuously Used

commit cd9c127069c040d6b022f1ff32fed4b52b9a4017 (patch) tree 61c346feb4d979fc120c6802a38104f14f948551 parent bf4a64b9323f181df8aba32d66cb37b9fa5df959 (diff)

#### Merge branch 'bpf-register-bounds-logic-and-testing-improvements'

Andrii Nakryiko says:

\_\_\_\_\_

BPF register bounds logic and testing improvements

This patch set adds a big set of manual and auto-generated test cases validating BPF verifier's register bounds tracking and deduction logic. See details in the last patch.

<b>Kernel Version</b>	<b>Solving Time</b>
v4.14	2.5h
v5.5	2.5h
v5.9	4h
v5.13	10h

#### Can we significantly reduce the solving time?

verifier l needed a b covered. l was incomp

We start

implementation of register bounds logic that tests in this patch set implement. So we need BPF verifier logic improvements to make all the tests pass. This is what we do in patches #3 through #9.

The end goal of this work, though, is to extend BPF verifier range state tracking such as to allow to derive new range bounds when comparing non-const registers. There is some more investigative work required to investigate and fix existing potential issues with range tracking as part of ALU/ALU64 operations, so  $\langle {\rm range} \rangle$  x  $\langle {\rm range} \rangle$  part of v5 patch set ([0]) is dropped until these issues are sorted out.

For now, we include preparatory refactorings and clean ups, that set up BPF verifier code base to extend the logic to <range> vs <range> logic in subsequent patch set. Patches #10-#16 perform preliminary refactorings without functionally changing anything. But they do clean up check\_cond\_jmp\_op() logic and generalize a bunch of other pieces in is\_branch\_taken() logic.

[0] https://patchwork.kernel.org/project/netdevbpf/list/?series=797178&state=\*

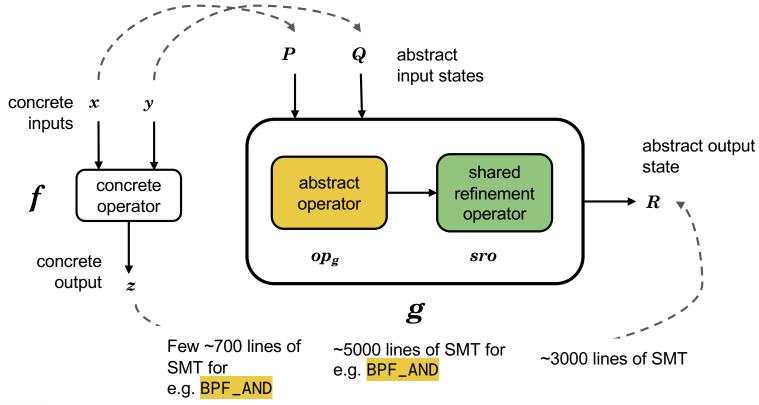
v5->v6:

- dropped <range> vs <range> patches (original patches #18 through #23) to

v6.4	several weeks
v6.5	timeout
v6.6	timeout
v6.7	timeout
v6.8	timeout



#### Why is Solving Time Slow?

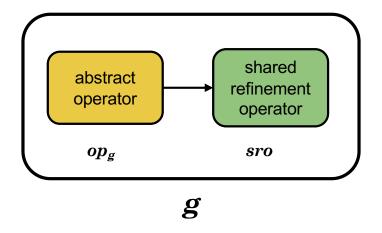




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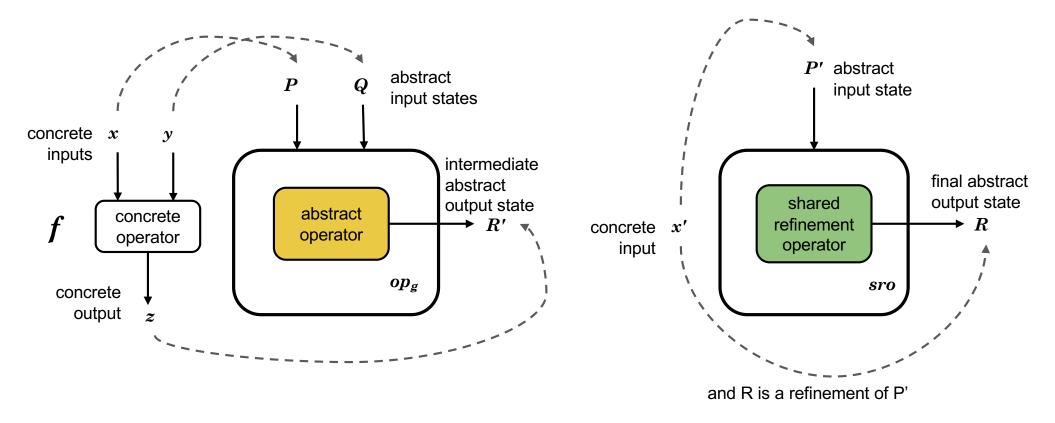
#### Divide and Conquer to Make Verification Feasible

#### Can we individually verify $op_g$ and sro ?



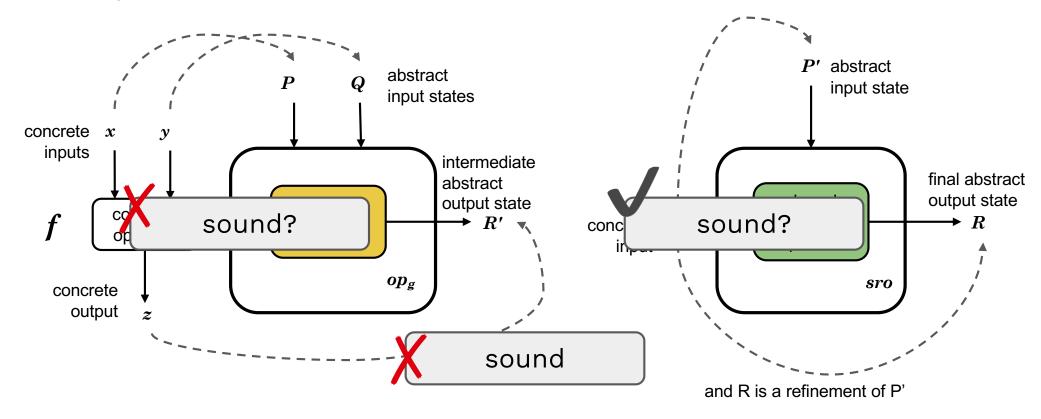


#### Divide and Conquer to Make Verification Feasible





#### Why Divide-and-Conquer Fails?





#### Latent Unsoundness in the Abstract Operators

```
case BPF_AND:
    out.tnum = tnum_and(in1, in2);
    out.s32, out.u32 = interval_and_32(in1, in2);
    out.s64, out.u64 = interval_and_64(in1, in2);
...
case BPF_OR:
    ...
out = sro(out);
```



#### Latent Unsoundness: interval\_and\_64

```
case BPF_AND:
         out.tnum = tnum_and(in1, in2);
         out.s32, out.u32 = interval_and_32(in1, in2);
         out.s64, out.u64 = interval_and_64(in1, in2);
       Obtaining Signed Interval Bounds from Unsigned Interval Bounds!
                                        1. def interval_and_64(in1, in2):
                                              out.u64_min = in1.tnum_value;
                                             out.u64_max = min(in1.u64_max, in2.u64_max);
                                             if (in1.s64_min < 0 || in2.s64_min < 0):
                                               out.s64_min = INT64_MIN;
                                               out.s64_{max} = INT64_{MAX};
                                        7. ► else:
                                              out.s64_min = out.u64_min;
                                        8.
                                              out.s64_max = out.u64_max;
Unsafe casting - unsigned to signed
```



#### Avoiding Latent Unsoundness: When is such Casting Safe?

Unsafe casting - unsigned to signed

1.  $s64_{min} = u64_{min}$ ;

2.  $s64_max = u64_max$ ;

#### Unsigned

 $u64_{min} \le u64_{max} \le 2^{63}-1$ 



 $u64_{min} \le 2^{63}-1 < u64_{max}$ 



#### Signed

 $0 \le s64 \text{ min} \le s64 \text{ max}$ 







#### Fixing Latent Unsoundness

```
def interval_and_64(in1, in2):
    ...
    out.u64_min = in1.tnum_value;
    out.u64_max = min(in1.u64_max, in2.u64_max);
    if (in1.s64_min < 0 || in2.s64_min < 0):
        out.s64_min = INT64_MIN;
        out.s64_max = INT64_MAY.
    else:
        sound?
    out.s64_max = out.u64_max;
    ...
...</pre>
```

```
def FIXED_interval_and_64(in1, in2):
    ...
    out.u64_min = in1.tnum_value;
    out.u64_max = min(in1.u64_max, in2.u64_max);
    if ((s64) out.u64_min <= (s64) out.u64_max):
        out.s64_min = INT64_MIN;
        out.s64_max = out.u64_max;
    ...
    sound?
    out.s64_max = out.u64_max;
    ...
...</pre>
```

Unsafe casting

Safe casting



#### Divide-and-Conquer Makes Verification Super Fast!

Kernel Version	Old Strategy Runtime	New Strategy Runtime
v4.14	2.5h	<5 min
v5.5	2.5h	<5 min
v5.9	4h	<5 min
v5.13	10h	<5 min
v5.19	36h	<15 min
v6.3	36h	<15 min
v6.4	several weeks	<15 min
v6.5	timeout	<15 min
v6.6	timeout	<15 min
v6.7	timeout	<15 min
v6.8	timeout	<30 min

BPF Instruction	Sound before patch?	Sound after patch?
bpf_and	×	V
bpf_and_32	×	V
bpf_or	×	V
bpf_or_32	×	V
bpf_xor	×	V
bpf_xor_32	×	V



#### Some Patches Upstreamed after Verification with Agni

```
author
                            Harishankar Vishwanathan <harishankar.vishwanathan@gmail.com>
                               Daniel Borkmann <daniel@iogearbox.net>
                  committer
                                                                          2024-04-16 17:55:27 +0200
                            1f586614f3ffa80fdf2116b2a1bebcdb5969cef8 (patch)
                  commit
                          7b5f4fa20fcbbdf316f4832c33d79dc8d4e8723d
                  tree
                            dac045fc9fa653e250f991ea8350b32cfec690d2 (diff)
                  parent
author
          Harish
                              bpf-next-1f586614f3ff.tar.gz
                  download
committer
             Dar
commit
          059247
                  bpf: Harden and/or/xor value tracking in verifier
        7dc40333
tree
```

parent e8e0f0f484780d7b90a63ea50020ac4bb027178d (diff) download bpf-next-05924717ac70.tar.gz

bpf, tnums: Provably sound, faster, and more precise algorithm for tnum\_mul





#### Improving the Precision of the Abstract Operators

```
* [PATCH bpf-next v4 1/2] bpf, verifier: Improve precision of BPF_MUL
  2024-12-18 3:23 [PATCH bpf-next v4 0/2] bpf, verifier: Improve precision of BPF_MUL Matan Shachnai
@ 2024-12-18 3:23 ` Matan Shachnai
  2024-12-18 3:23 ` [PATCH bpf-next v4 2/2] selftests/bpf: Add testcases for BPF_MUL Matan Shachnai 2024-12-30 23:00 ` [PATCH bpf-next v4 0/2] bpf, verifier: Improve precision of BPF_MUL patchwork-bot+netdevbpf
  2 siblings, 0 replies; 4+ messages in thread
From: Matan Shachnai @ 2024-12-18 3:23 UTC (permalink / raw)
  Cc: harishankar.vishwanathan, srinivas.narayana, santosh.nagarakatte,
        m.shachnai, Matan Shachnai, Daniel Borkmann, John Fastabend,
        Andrii Nakryiko, Martin KaFai Lau, Eduard Zingerman, Song Liu,
        Yonghong Song, KP Singh, Stanislav Fomichev, Hao Luo, Jiri Olsa,
        Mykola Lysenko, Shuah Khan, Cupertino Miranda, Menglong Dong, bpf,
        linux-kernel linux-kselftest
                                                                                                   Upstreamed a few months ago to
This patch improves (or maintains) the precision of register value tracking
                                                                                                                          bpf-next
in BPF_MUL across all possible inputs. It also simplifies
scalar32 min max mul() and scalar min max mul().
As it stands, BPF_MUL is composed of three functions:
case BPF MUL:
  tnum_mul();
  scalar32_min_max_mul();
  scalar_min_max_mul();
The current implementation of scalar_min_max_mul() restricts the u64 input
ranges of dst_reg and src_reg to be within [0, U32_MAX]:
    /∗ Both values are positive, so we can work with unsigned and
     * copy the result to signed (unless it exceeds S64_MAX).
    if (umax_val > U32_MAX || dst_reg->umax_value > U32_MAX) {
        /* Potential overflow, we know nothing */
         __mark_reg64_unbounded(dst_reg);
        return;
```



#### **Looking Ahead?**

Specify the verifier at a higher level of abstraction?

Verifier in user space?

**Automatically Checking the Precision of Operators?** 

A compiler explorer like framework for the eBPF verifier? Patches with correctness arguments



## "Always-on" Lightweight Formal Methods have the potential to make the eBPF verifier robust



#### **Open Source**

Visit the Agni GitHub page for details: <a href="https://github.com/bpfverif/agni">https://github.com/bpfverif/agni</a>







